

# Incorporating geometry into machine learning models

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Joint work with Viacheslav Borovitskiy,\* Iskander Azangulov,\*  
Peter Mostowsky,\* and Marc Deisenroth

Talk for TheAlgo

November 12<sup>th</sup>, 2020

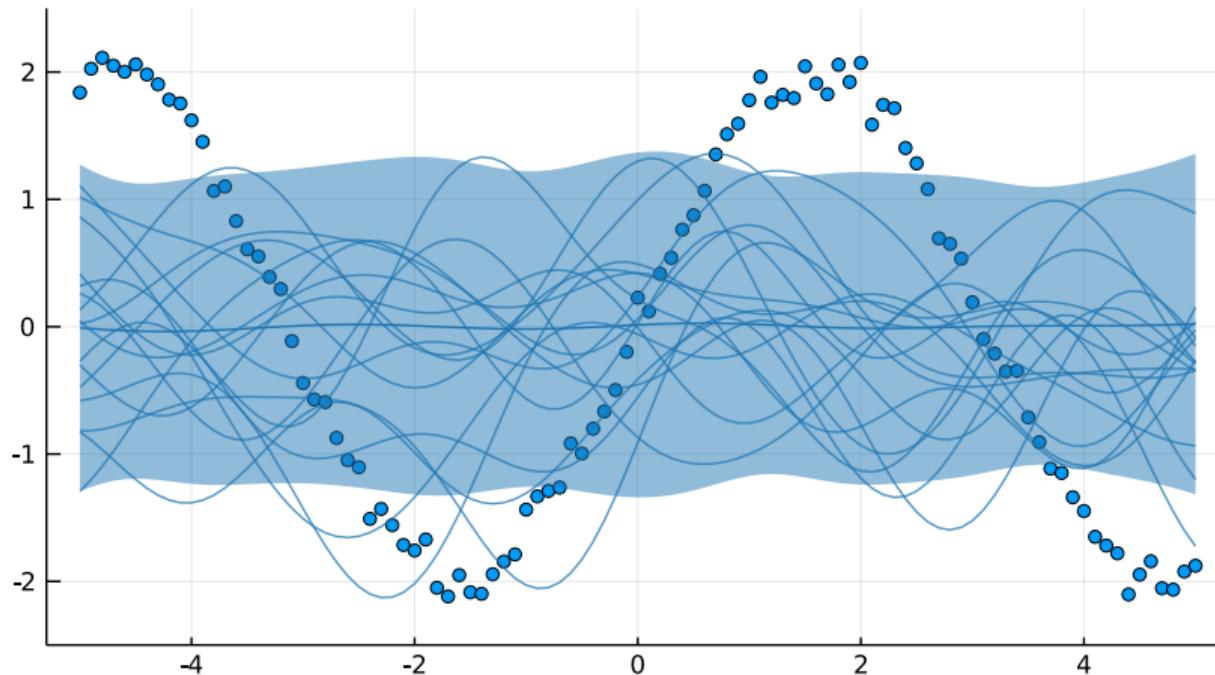
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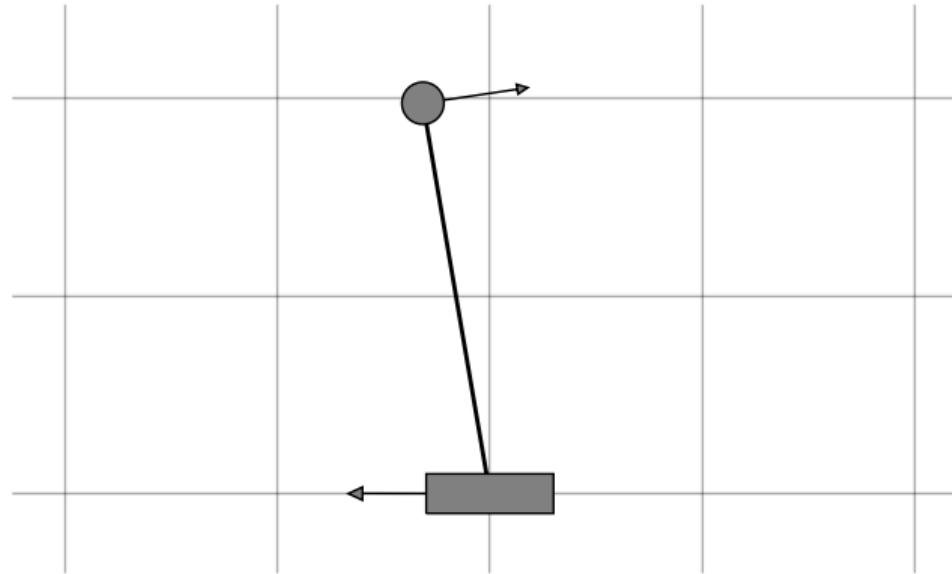
\*Equal contribution

 UCL

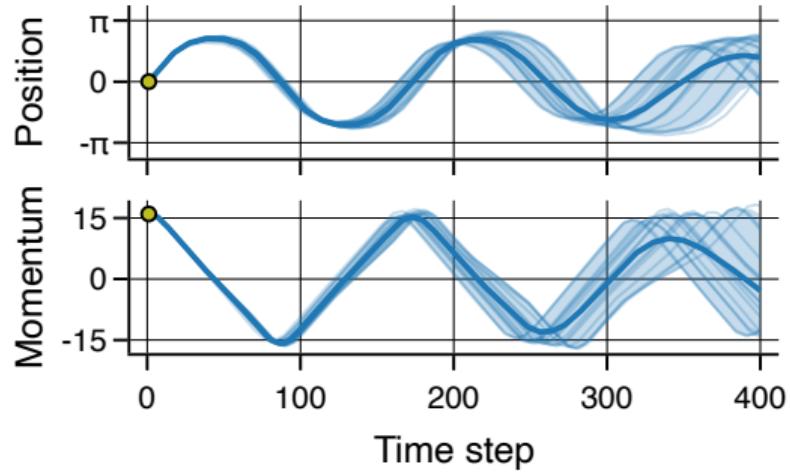
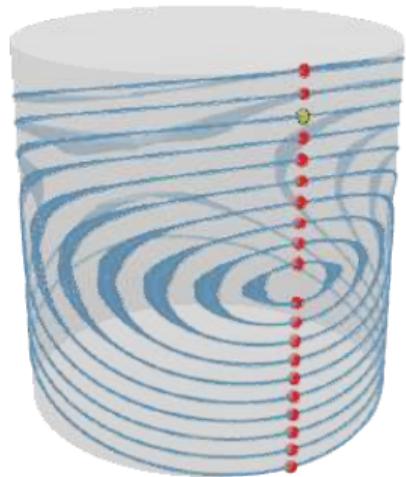
# Gaussian processes



# Modeling dynamical systems



# Modeling dynamical systems



# Matérn Gaussian processes on Riemannian manifolds

Viacheslav Borovitskiy\*, Alexander Terenin\*, Peter Mostowsky\*, and Marc Deisenroth



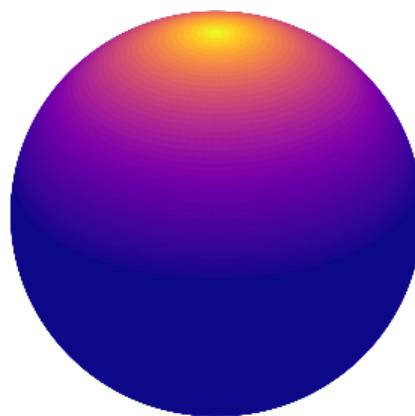
\*Equal contribution

# Matérn Gaussian processes on Riemannian manifolds

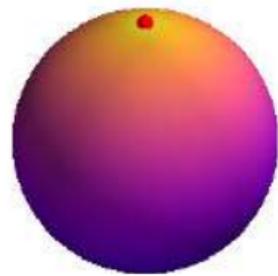
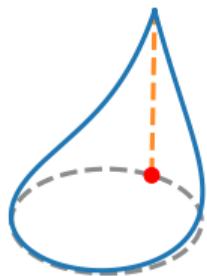
$$f : M \rightarrow \mathbb{R}$$

$M$ : Riemannian manifold (circle, sphere, cylinder, many others)

Key technical tools: stochastic partial differential equations and spectral theory



## Dependence between nearby points



## Trained models



(a) Ground truth



(b) Posterior mean

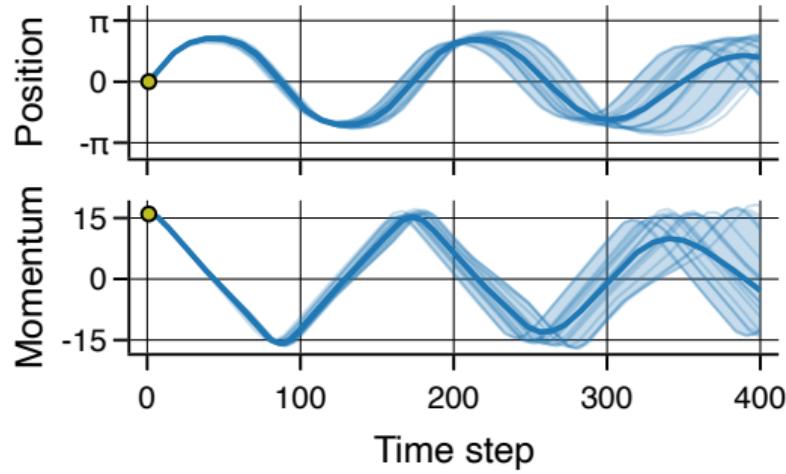
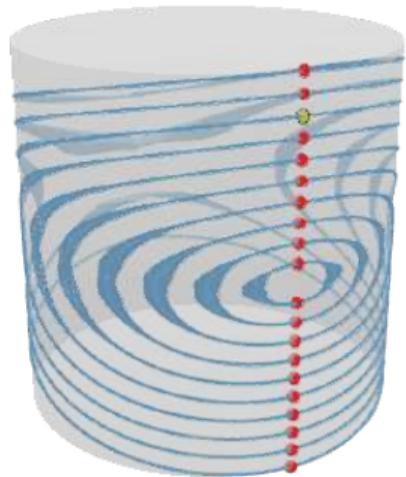


(c) Standard deviation



(d) One posterior sample

# Modeling dynamical systems



# Matérn Gaussian processes on Graphs

Viacheslav Borovitskiy\*, Iskander Azangulov\*, Alexander Terenin\*,  
Peter Mostowsky, Marc Deisenroth, and Nicolas Durrande



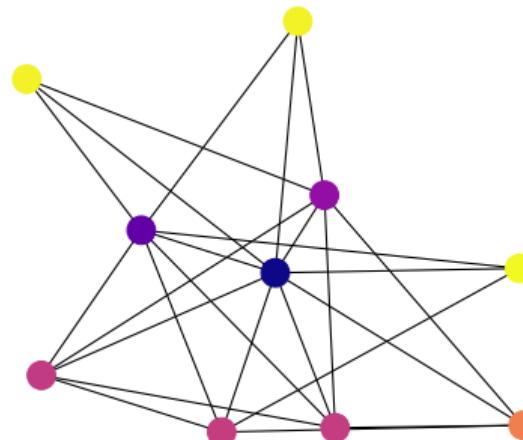
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# Matérn Gaussian processes on Graphs

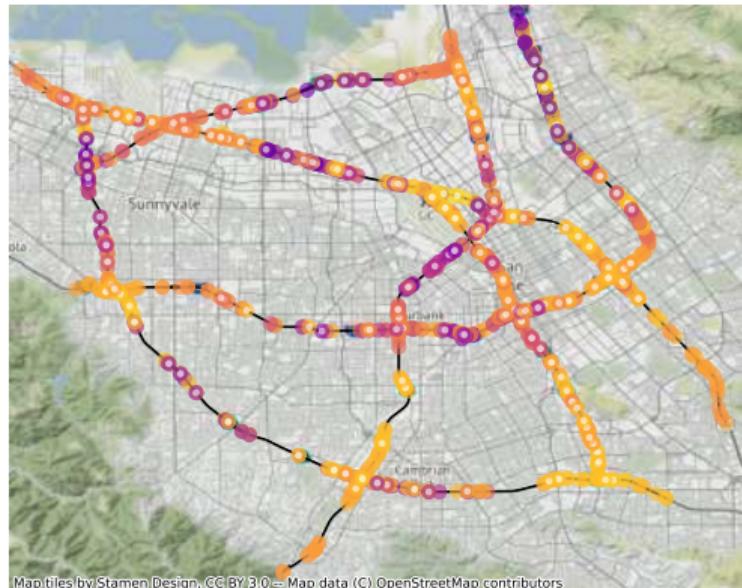
$$f : G \rightarrow \mathbb{R}$$

$G$ : weighted undirected graph

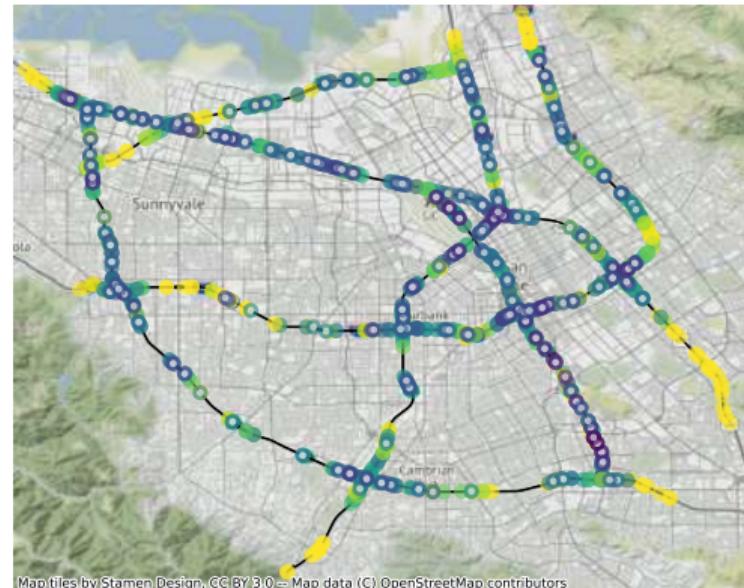
Key technical tools: graph Laplacian and spectral theory



# Trained models



(a) Predictive mean



(b) Standard deviation

# Trained models

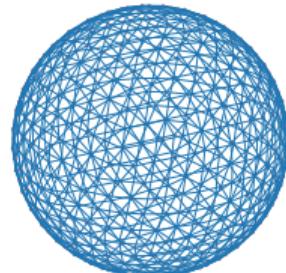
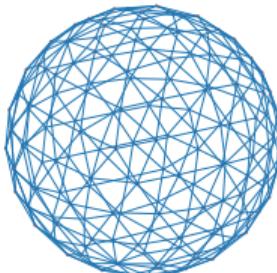
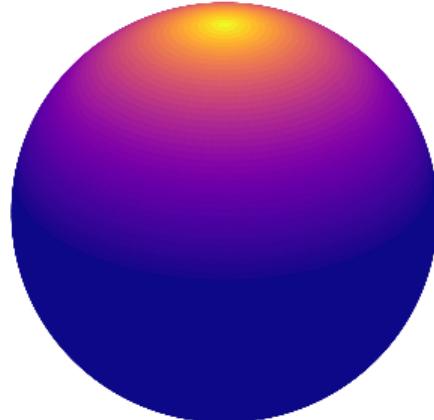
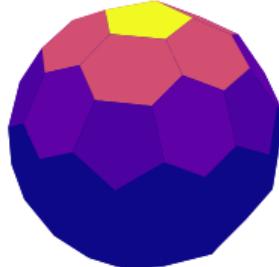


(a) Predictive mean



(b) Standard deviation

## Convergence to manifold limit



# Concluding remarks

Thank you for your attention!

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V. Borovitskiy\*, A. Terenin\*, P. Mostowsky\*, M. P. Deisenroth. Matérn Gaussian Processes on Riemannian Manifolds. Advances in Neural Information Processing Systems, 2020. \*Equal contribution.

V. Borovitskiy\*, I. Azangulov\*, A. Terenin\*, P. Mostowsky, M. P. Deisenroth, N. Durrande. Matérn Gaussian Processes on Graphs. arXiv:2010.15538, 2020. \*Equal contribution.