

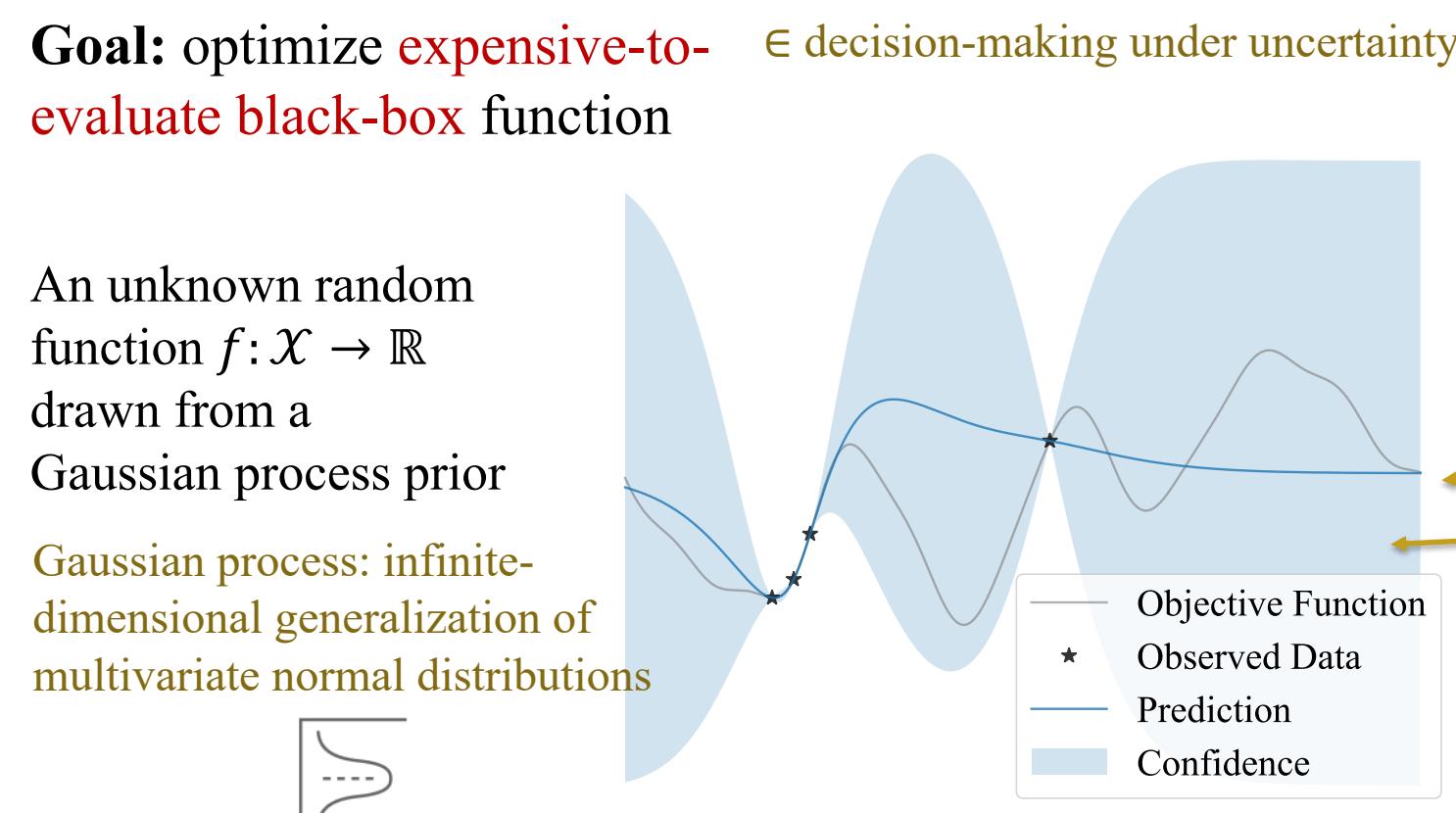
Cost-aware Bayesian Optimization via the Pandora's Box Gittins Index

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Introduction to Bayesian Optimization



Applications:
Hyperparameter tuning
Drug discovery
Control design
 x : hyperparameter/configuration

mean: prediction
variance: confidence/uncertainty

Trade-off between
• exploitation (high mean)
• exploration (high uncertainty)

Objective: find global optimum $x^* = \operatorname{argmax}_{x \in \mathcal{X}} f(x)$

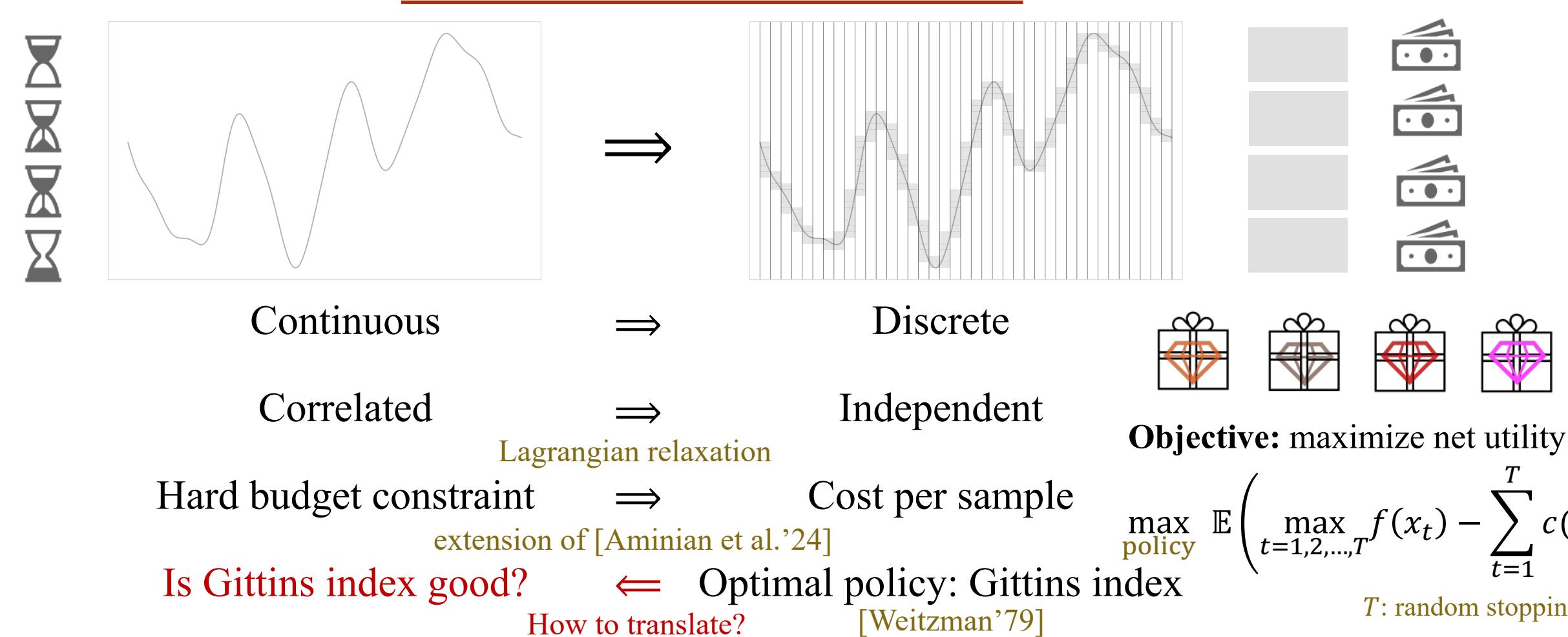
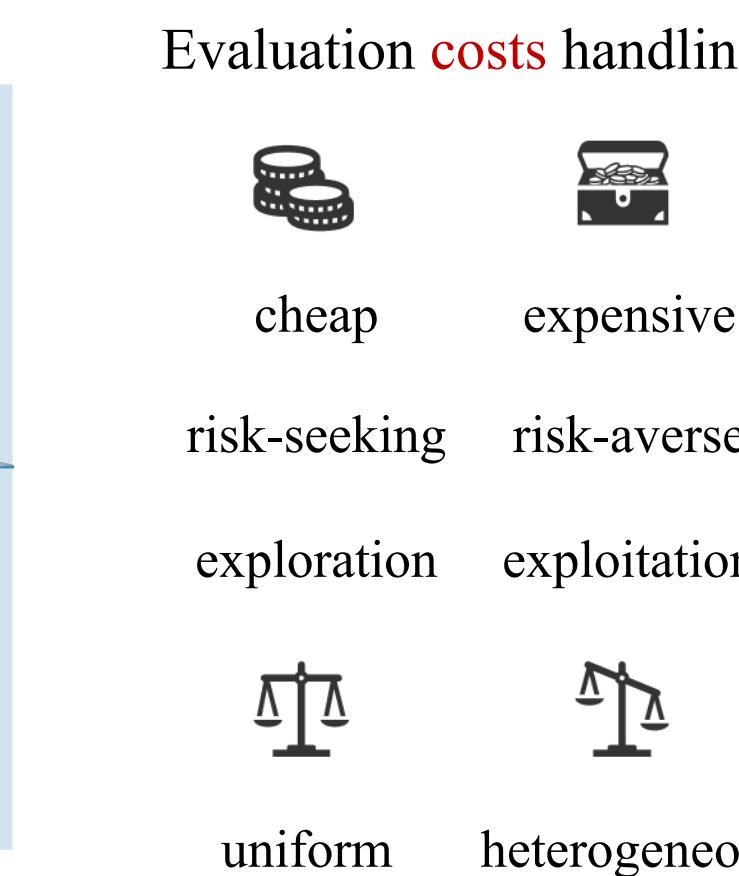
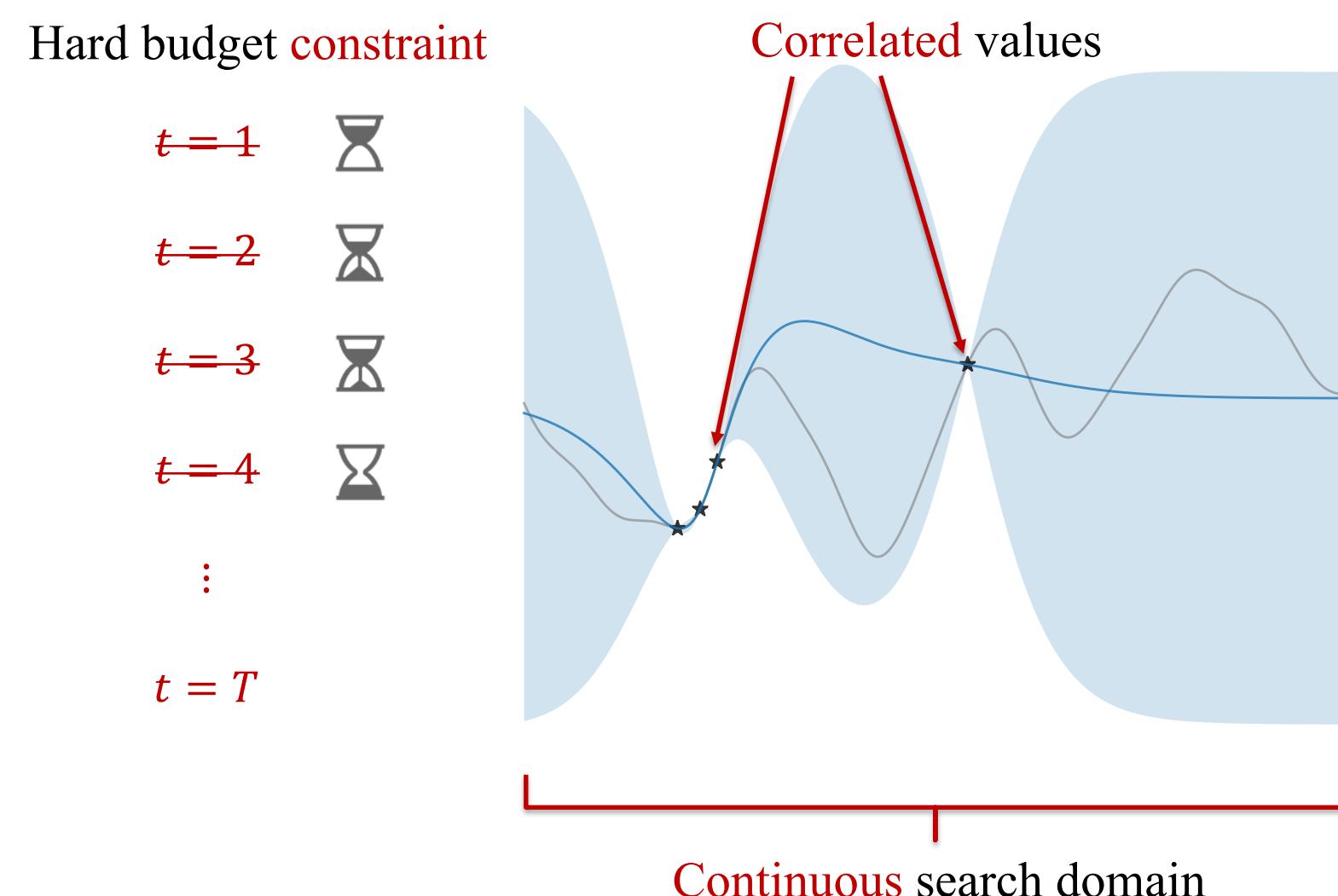
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Objective: optimize best observed value at time T

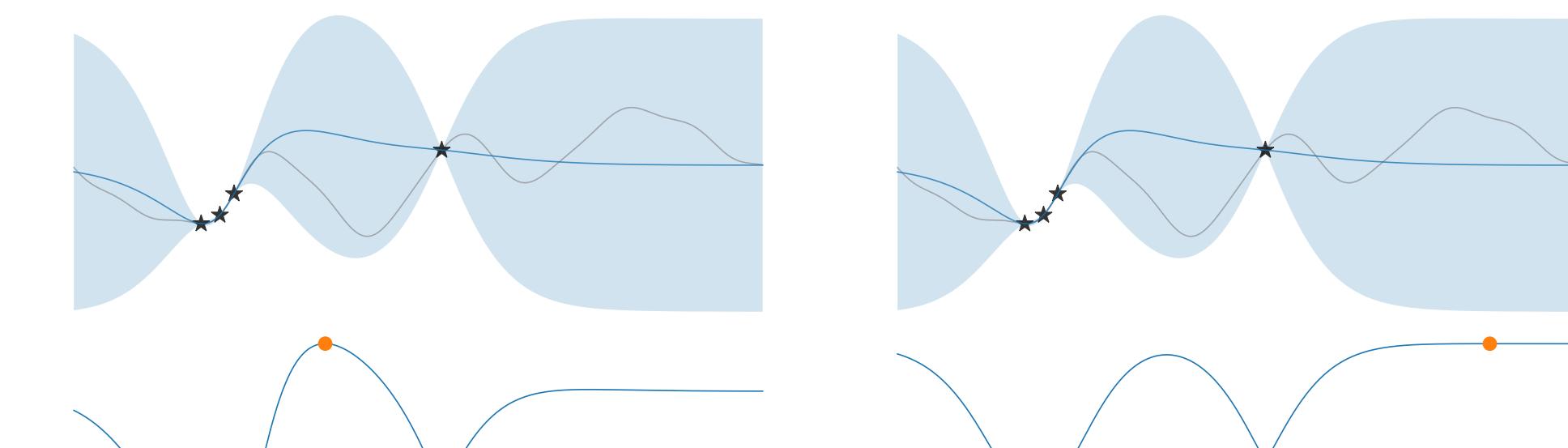
max policy $\mathbb{E} \max_{t=1,2,\dots,T} f(x_t)$

Decision: evaluate a set of points
↓
Decision: adaptively evaluate $x_1, x_2, \dots, x_T \in \mathcal{X}$ given time budget T

Why is Bayesian Optimization Hard?



Acquisition Functions



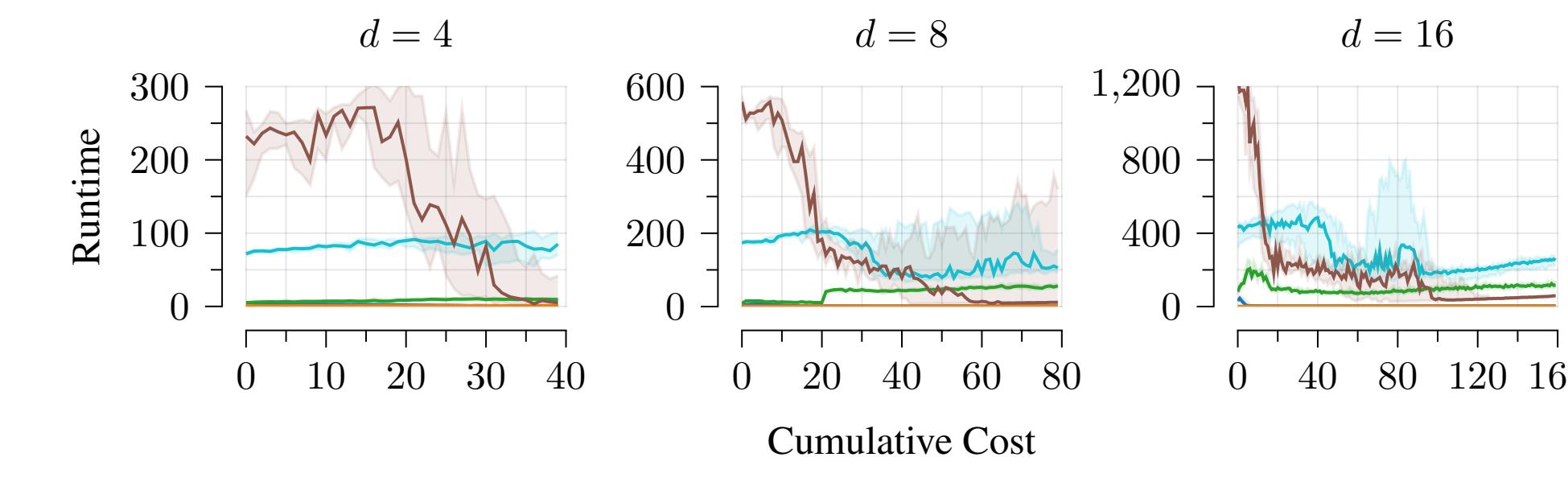
Expected Improvement (EI)
 $\text{EI}_{f|D}(x; y) = \mathbb{E}[(f|D)(x) - y]^+$

EI policy: evaluate $\operatorname{argmax}_x \text{EI}_{f|D}(x; y_{\text{best}})$

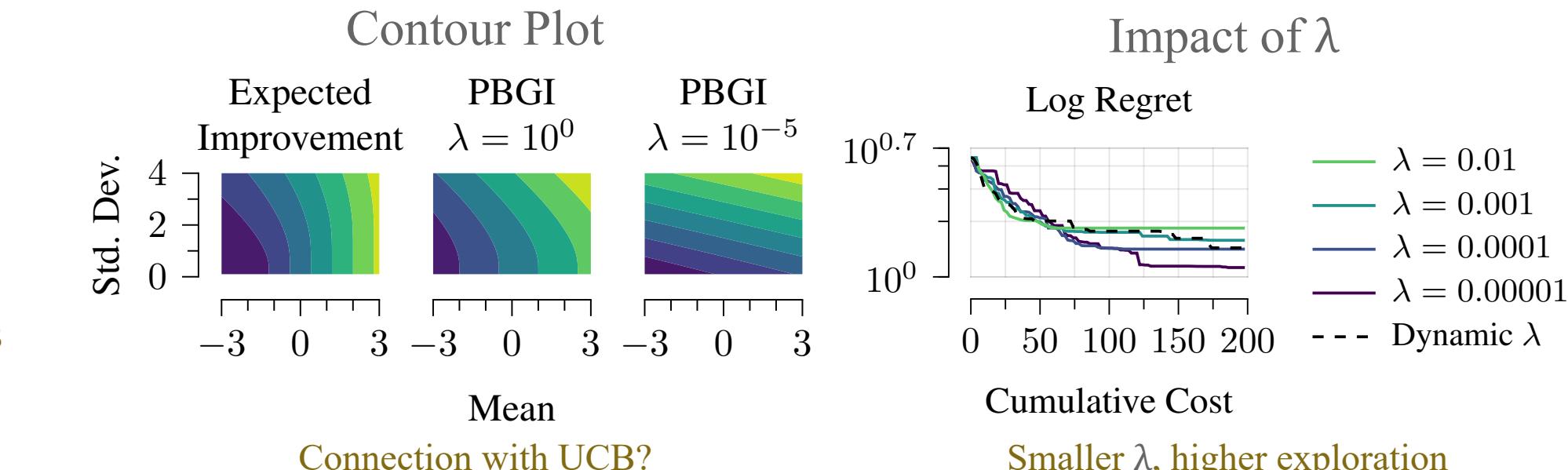
D : observed data, y_{best} : current best observed value

Other acquisition functions:

- Upper Confidence Bound (UCB)
- Thompson Sampling (TS)

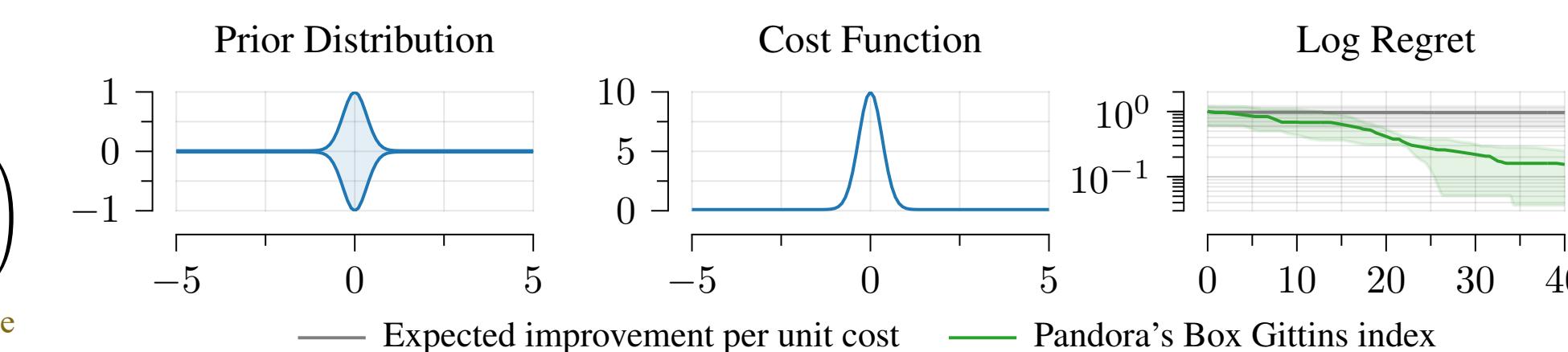


PBGI is easy to compute using bisection method!

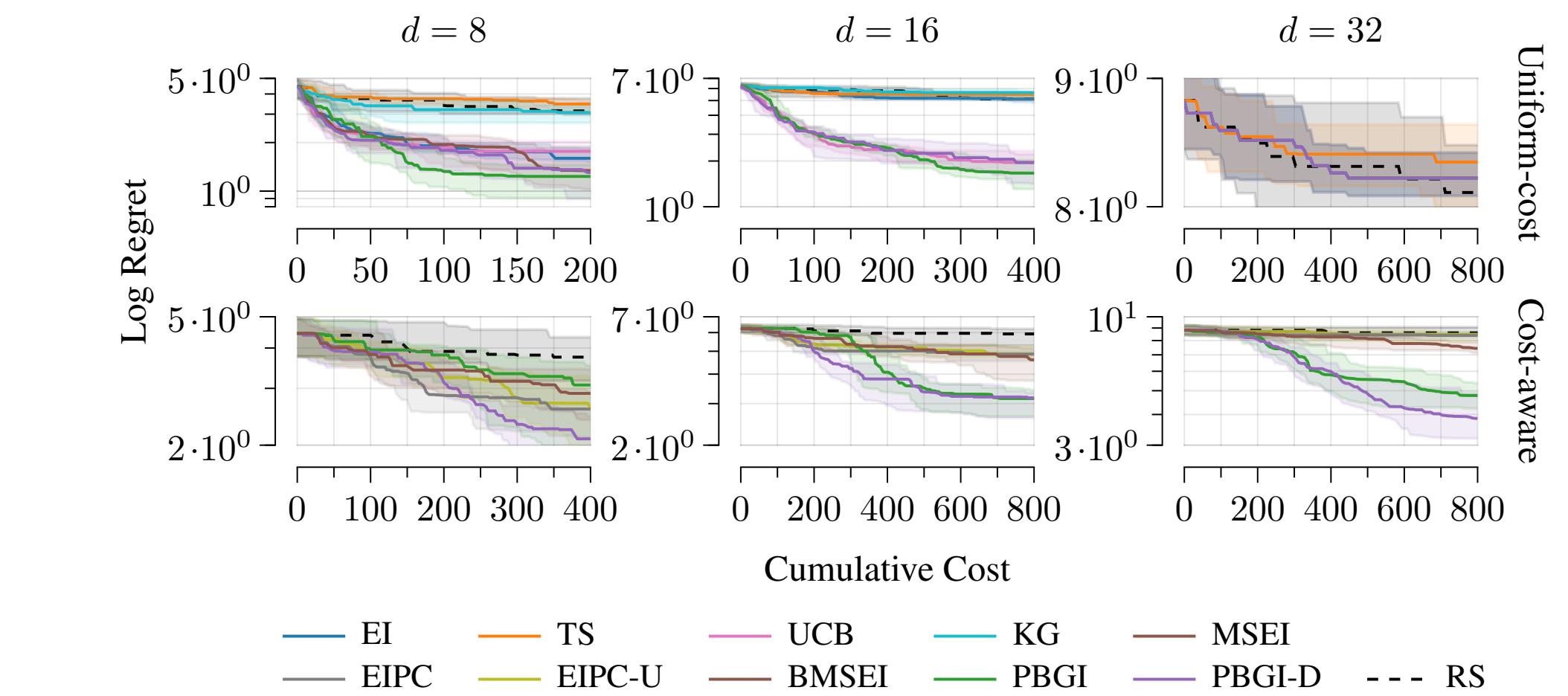


Heterogeneous Costs

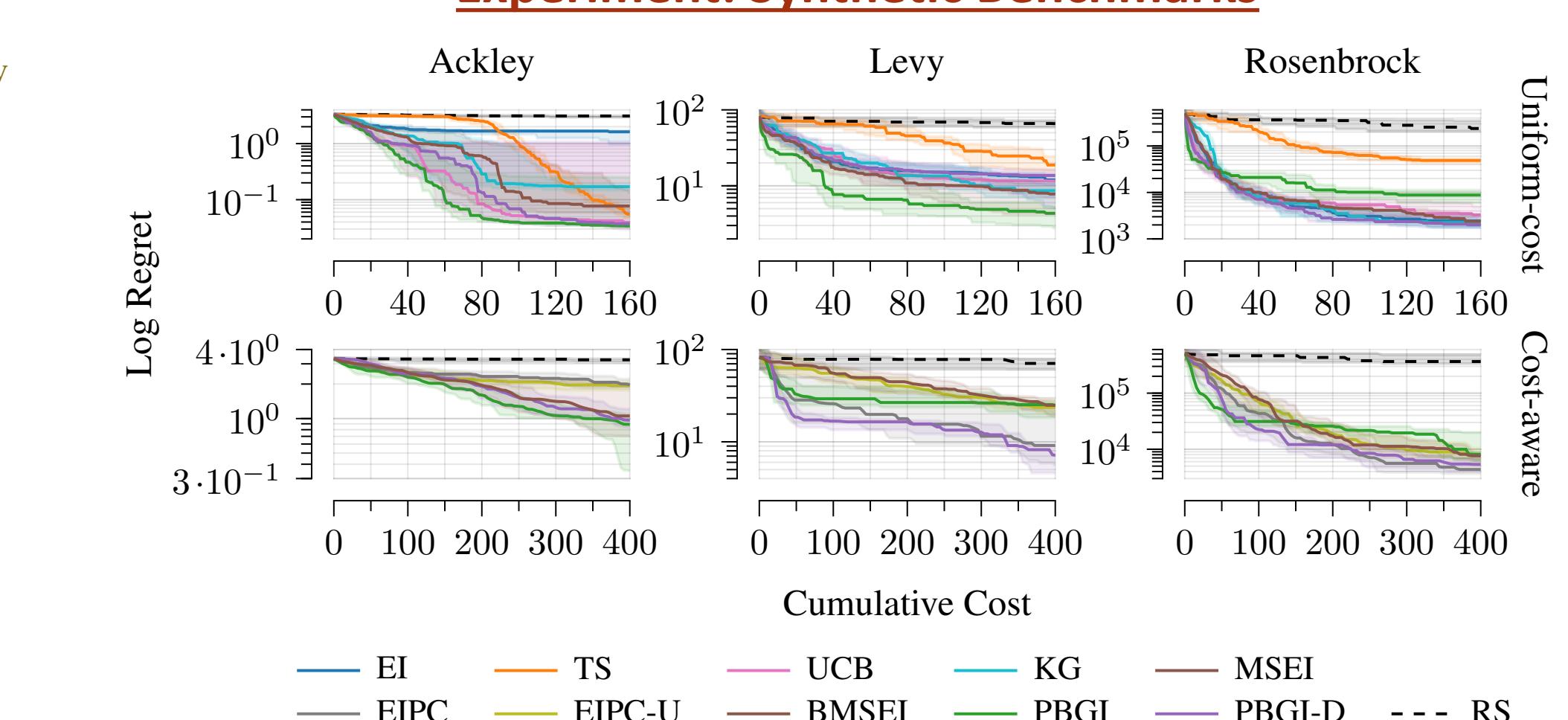
- Given cost function $c: \mathcal{X} \rightarrow \mathbb{R}^+$ and budget B
- Replace λ with $\lambda c(x)$ to compute $g(x)$ as PBGI



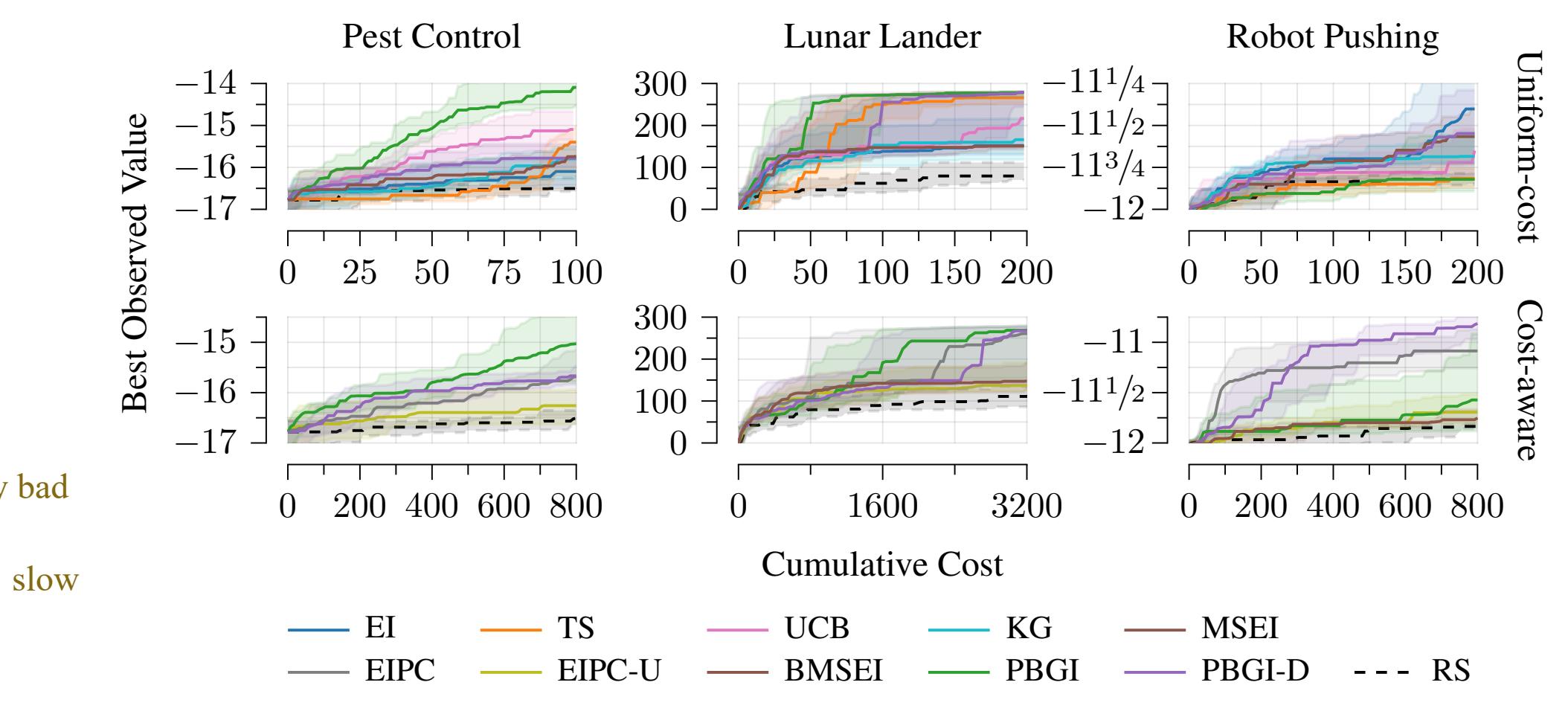
Experiment: Bayesian Regret



Experiment: Synthetic Benchmarks



Experiment: Empirical



Future Work

Extension to complex BO (freeze-thaw, multi-fidelity, function network, etc.) via Gittins variants (“golf” Markovian MAB, optional inspection, etc.)