

## **Cost-aware Bayesian Optimization via the Pandora's Box Gittins Index**

Qian Xie,<sup>1</sup> Raul Astudillo,<sup>2</sup> Peter Frazier,<sup>1</sup> Ziv Scully,<sup>1</sup> and Alexander Terenin<sup>1</sup> <sup>1</sup>Cornell University <sup>2</sup>Caltech

## **Abstract**

Bayesian optimization is a technique for efficient global optimization of black-box unknown functions. In many practical settings, it is desirable to explicitly incorporate function evaluation costs into acquisition functions used for Bayesian optimization. To do so, we develop a connection between cost-aware Bayesian optimization and Pandora's Box, a decision problem from economics. The Pandora's Box problem admits a Bayesian-optimal solution based on an expression called the *Gittins index*, which can be reinterpreted as an acquisition function. We demonstrate empirically that this acquisition function performs well on cost-aware Bayesian optimization, particularly in medium-high dimensions. We further show that this performance carries over to classical Bayesian optimization without explicit evaluation costs. Our work constitutes a first step towards integrating techniques from Gittins index theory into Bayesian optimization.





Key difference from Bayesian optimization: no correlations

## Pandora's Box Gittins Index: a new acquisition function

 $\alpha_{\star}^{\text{PBGI}}(x) = q$ where g solves  $\operatorname{EI}_{f|x_{1:t},y_{1:t}}(x;g) = \lambda c(x)$ 

q

Idea: extend  $\alpha^*$  by plugging posterior in for f $\lambda$ : cost scaling factor from budget-constraint Lagrangian duality Computation: one-dimensional convex optimization





Dev.

Std.











